

## Temporal Analysis of Topic Modeling Output by Machine Learning Techniques

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### Abstract

Topic modeling is widely recognized as one of the most effective and significant methods of unsupervised text analysis. This method facilitates identifying and extracting topics in document sets associated with various entities (e.g., countries, websites, journals, etc.). Nonetheless, the method's output lacks high-level information per entity. Applying machine learning methods to topic modeling outputs is generally challenging. Some studies have already applied machine learning methods statically, ignoring the effect of time on topic modeling outputs. The inclusion of time introduces additional complexity to the problem. This study introduces a novel approach to clustering the output of topic modeling per entity, considering the time factor. Topic popularity over time and the feature vector for each entity over time are proposed for this purpose. Due to the high dimensionality of the proposed feature vector, selecting an appropriate dimension reduction technique and the corresponding clustering algorithm may not be a straightforward task. This research proposes a new approach to selecting a dimensionality reduction method and its corresponding clustering technique. A case study is conducted on COVID-19-related tweets to evaluate the proposed method's performance. The proposed approach applies t-distributed stochastic neighbor embedding (t-SNE) for dimensionality reduction and Fuzzy C-Means (FCM) for clustering. While our study incorporates the time factor, unlike previous research, it also outperforms them in terms of the Davies-Bouldin Index (DBI), Silhouette Coefficient (SC), Calinski-Harabasz Index (CHI), and Dunn Index (DI) parameters. The proposed method enables researchers in natural language processing to analyze topic dynamics across various entities, leading to improved research outcomes.

**Keywords:** Topic modeling, Natural language processing, Clustering, Social network, Covid-19.

### 1. Introduction

Topic modeling [1] is widely recognized as a highly effective and significant technique for unsupervised text analysis. This method enables the identification of topics in document sets and their extraction from various texts, such as research article abstracts [2] and social network user comments [3]. In topic modeling, words' weights are extracted to identify significant and frequently occurring words. Nonetheless, these weights alone do not offer high-level information and necessitate additional analysis and processing through machine learning techniques. Applying machine learning techniques to the output of topic modeling can be challenging, especially when dealing with big textual data that represent different entities over time (e.g., countries, journals, and authors).

Formally, let's consider a scenario where we have a collection of X texts (e.g., tweets, paragraphs, or documents) related to Y entities (e.g., countries, websites, or journals). These texts are associated with

various time slots. Topic modeling, as a method, statically provides the topics of the texts and their associated word probabilities as output. However, it does not account for the time factor or offer additional insights about the entities themselves. This leads to the crucial question of extracting higher-level information from the outputs of topic modeling. In other words, topic modeling alone does not analyze the entities directly over time. Consequently, another question arises: how can we effectively cluster the entities using the topic modeling output?

Previous research has presented static analyses on topic modeling output. In this context, Euclidean methods [4] and Jensen-Shannon divergence (JSD) [2, 5] have been used to cluster entities based on their static distributions of topics. However, the primary challenge arises when considering the element of time. Indeed, the static clustering of entities, without taking into account the time factor, will not yield accurate results. In numerous applications, the topics of entities undergo changes over time. Figure 1 presents the temporal changes in certain topics related to COVID-19 pandemic in the United States of America (USA). Specifically, the topics of Vaccine, Masking, and Work & telecommuting are highlighted. Incorporating the element of time will increase the complexity of the problem. To the best of our knowledge, none of the previous research studies have taken the time factor into consideration [2, 4, 5].

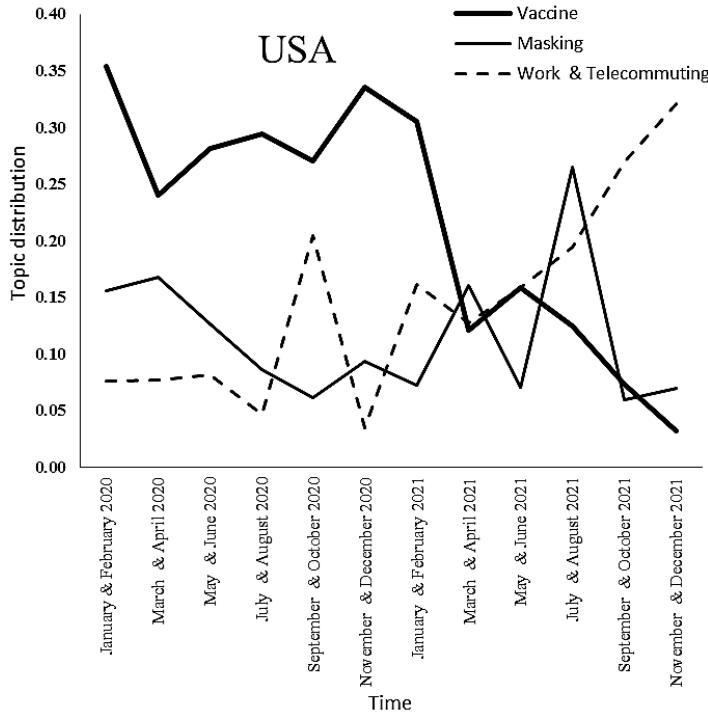


Figure 1 Distribution of three topics of the USA over time.

Continuing previous work [3], this study proposes a new method for clustering the output of topic modeling over time and per entity. Given that one of the largest, most significant, and most widely-discussed text datasets in recent years pertains to COVID-19, our topic modeling analysis focuses on a dataset of tweets about COVID-19 for 2020 and 2021. To consider the time factor, we introduce a parameter of the popularity of topics over time. This parameter is then utilized to propose a temporal feature vector for each entity (country). Given the large dimensions of the proposed feature vector, it is necessary to select a dimension-reduction technique for big datasets. Moreover, an optimal clustering method must be selected. Selecting the appropriate combination of dimension-reduction and clustering methods can be a daunting task. This study proposes an approach to selecting a pair of dimension-

reduction and clustering methods based on DBI [6], SC [7], CHI [8], and DI [9] clustering evaluation criteria.

After applying the proposed method, the t-SNE [10] technique was selected for dimension reduction, and the FCM [11] algorithm was chosen for clustering. While previous research overlooked the time factor, the results of the proposed method show promising performance in comparison to previous methods, as indicated by favorable evaluation parameters, including DBI, SC, CHI, and DI. In summary, the main contributions of this research are outlined as follows:

- Proposing a temporal clustering scheme of the output of topic modeling.
- Proposing a pair selection method for dimension reduction and clustering.

These outcomes offer valuable insights for natural language processing researchers, enabling them to better understand the dynamics of topic analysis for various entities and potentially improve the accuracy of their research findings.

The article is organized as follows. Section 2 provides a comprehensive review of the research background. The methodological approach is detailed in Section 3. Section 4 presents the research experiments, including comparing the proposed method with previous methods. Finally, Section 5 provides a summary and conclusion.

## 2. Related work

Words are arranged in accordance with syntactic patterns to form sentences, and these sentences collectively constitute a text in relation to one another. When considering all the sentences in a text, one encounters a complex communication structure and a collection of explicit and implicit relationship concepts [12]. Topic modeling is a widely used method for discovering implicit relationships in texts [3].

Autoencoders are a type of the topic modeling method that aim to learn a low-dimensional representation of the input data by encoding it into a latent space. This latent space is then used to extract topics or themes present in the text. Autoencoders work by capturing the underlying patterns in the data through neural networks or other machine learning algorithms. Variational autoencoders (VAE) [13] are one of the recent popular algorithms for topic modeling [14]. This encoder has been used in various fields, including emotion classification [15, 16], sentiment classification [17], Information extraction enhancement [18], and conversational semantic role labeling enhancement [19]. With the help of VAE, various goals such as reducing the computational cost of computing the posterior distribution [14], improving multi-label emotion classification [15, 16], improving sentiment classification at the document level [17], and improving information extraction [18] have been realized.

On the other hand, Latent Dirichlet Allocation (LDA) is a popular probabilistic generative model for topic modeling [3]. LDA is based on the assumption that each document composed of a combination of a group of topics, and each word in the document is generated from one of these topics. By inferring the underlying topic structure from the observed word distributions, LDA is able to identify the topics present in a given text corpus [3]. This approach has been successfully applied in diverse fields, such as geography [20], psychology [3], news [21], and economics [22]. Through topic modeling, several objectives have been achieved with minimal human intervention. These include the identification of current and prevalent research topics [23], enhancement of search capabilities within the portal of the Federal Digital Libraries of the USA [24], and the development of an ontology graph [25].

While both autoencoders and LDA can be used for topic modeling, LDA has been shown to have several advantages over autoencoders. One key advantage of LDA is its interpretability. Since LDA is based on a probabilistic generative model, the resulting topics are easily interpretable as distributions over

words. This allows users to understand and analyze the topics discovered by LDA more easily compared to the latent representations learned by autoencoders. Additionally, LDA is robust to noise and sparse data, making it well-suited for working with real-world text data that often contains noise and missing information. Its probabilistic framework also provides a principled way to model uncertainty and capture the inherent variability in language data. Overall, while both autoencoders and LDA can be effective for topic modeling, LDA's interpretability, robustness, and probabilistic nature make it a superior choice for extracting meaningful and interpretable topics from text data.

Afterall, analyzing topic modeling outputs, particularly through clustering, is a new research area. Since topic modeling is unsupervised and lacks labeled data, clustering becomes a crucial analysis. Only a few studies have explored topic modeling results using clustering, which will be discussed in detail below.

To cluster countries based on their article publication patterns in the field of environmental science, researchers gathered a dataset of more than 3000 articles published from 2005 to 2019 from relevant journals [4]. The LDA (Latent Dirichlet Allocation) topic modeling method [26] was utilized to analyze the abstracts of these articles, leading to the identification of 20 topics, such as environmental impact assessment and improved clean cookstoves. The topic ratios' distributions were statically calculated using LDA for 17 countries, and Euclidean distances were employed to measure the dissimilarities between these distributions. Finally, hierarchical clustering was applied to cluster the countries based on these distances.

Similarly, for clustering countries based on their publishing patterns in the field of structural engineering, researchers gathered a dataset comprising over 51,000 articles published from 2000 to 2020 from relevant journals [5]. The LDA topic modeling method was applied to the abstracts, resulting in the identification of 50 topics, such as structural control, wind flow, and turbulence. The distributions of these topics across 31 countries were calculated statically using LDA, and the JSD (Jensen-Shannon Divergence) parameter was used to determine the distances between the topic distributions. Ultimately, hierarchical clustering was employed to cluster the countries based on these distances.

Finally, more than 17,000 articles published in journals in the field of transportation between 1990 and 2015 have been compiled for the purpose of clustering countries based on their article publication patterns [2]. The LDA algorithm was used to analyze the abstracts of these articles, resulting in the identification of 50 topics, such as travel behavior and non-motorized mobility. Next, the distributions of topic ratios in 32 countries were determined using LDA. Additionally, the distances between these distributions were calculated using JSD. Finally, the distances were clustered using the hierarchical clustering method.

None of the above studies have included the time factor when analyzing the outputs of topic modeling for entity clustering. Indeed, the entity of countries in previous research is statically clustered. The clustering process has ignored the fact that topics change over time. The static analysis of the datasets results in the loss of a significant portion of the information (Figure 1).

### 3. Proposed Clustering Method

The topic modeling method proposed in previous research [3] was initially employed to extract relevant topics. Following that, the concept of topic popularity is introduced, and based on that, the feature vector derived from the output of topic modeling over time is proposed for countries. Next, the proposed approach to select the suitable method for dimension reduction, clustering, and cluster number determination is introduced. Ultimately, the clustering results are presented. The outline of the proposed method is provided in Figure 2.

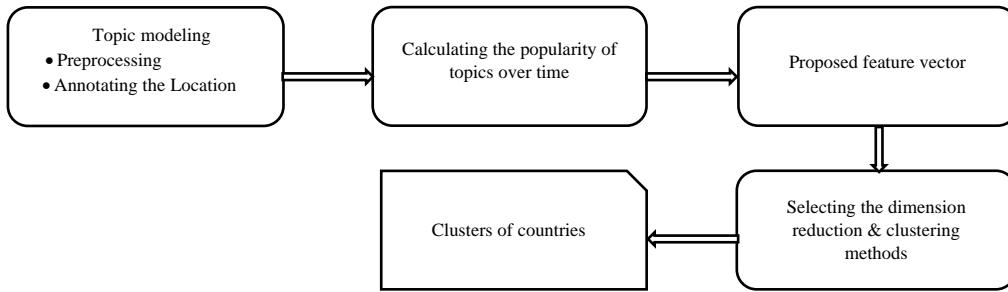


Figure 2 The outline of the proposed method

A case study is conducted on a dataset containing 14 million tweets (in 2020 and 2021) related to COVID-19. Then, 120,000 tweets are randomly selected for every two-month period to normalize the dataset. Ultimately, the dataset contains a total of 1,440,000 tweets for 12 two-month periods in 2020 and 2021. After applying topic modeling [3], the word cloud of each cluster is utilized to determine each topic's title [5]. To this end, larger words carry more significance, and the selection of each cluster's name is based on the larger words in the word cloud. Below are the keywords and the chosen name for each topic.

Masking = {mask, wear, gloves, protects, facemasks, spread, face}  
 Cases and death cases = {confirm, case, death, passed, highest}  
 Spread = {variant, global, spread, outbreak, infect}  
 Work and telecommuting = {office, work, home, workplace, employ}  
 Students and education = {children, university, student, college, exam}  
 Vaccine = {scientist, passport, vaccine, immunity}  
 Power and politics = {Biden, president, Trump, government}  
 Economy = {business, economy, market, work}  
 Voluntary affairs = {service, humanity, warrior, volunteer, member}  
 Plasma = {plasma, therapy, donors, recovery, immunity, blood}

### 3.1.1. Popularity of topic

After topic extraction, topic popularity is proposed as a means to extract features from the results of topic modeling over time. This concept demonstrates the weight of a topic in relation to other topics in a specific period, achieved through the analysis of topic distributions over time. In other words, the popularity of topic K in the  $t^{\text{th}}$  two-month period depends on the number of tweets that contain this topic during this period to the total number of tweets in this period. Therefore, by utilizing the concept of topic popularity, we can easily compute and analyze the impact and significance of topic K during time t. The popularity of topic K in the  $t^{\text{th}}$  two-month period ( $p_K(t)$ ) is defined as the ratio of the number of tweets related to topic K to the total number of tweets in this period:

$$(p_K(t)) = \frac{\text{Tweets related to topic K in the } t^{\text{th}} \text{ 2-month period}}{\text{Tweets in the } t^{\text{th}} \text{ 2-month period}} \quad (1)$$

The popularity of topic K throughout the entire period demonstrates the total extent to which topic K has been addressed and how popular it has been among users.  $P_K$ , the popularity of topic K over the entire period, is defined as follows:

$$P_K = \sum_{t=1}^{12} p_K(t) \quad (2)$$

### 3.2. Proposed feature vector

In order to apply the machine learning techniques to the topic modeling results, it is necessary to model countries as feature vectors that consider the time trend. If the objective of using machine learning methods is to perform a static analysis of topics over the entire period,  $P_K$  would be sufficient for any topic, as it takes the entire period into account. However, since the time factor is particularly important in most research studies, the feature vector consists of a sequence of  $p_k(t)$ s. Indeed, a feature vector of topic popularity values over time intervals is proposed for each country. In this case study, the feature vector is formed with a length of 120 for this purpose:

$$\text{Feature vector of a country} = \{p_1(1), p_1(2), \dots, p_1(12), \dots, p_{10}(1), p_{10}(2), \dots, p_{10}(12)\} \quad (3)$$



The popularity of the first topic in subsequent intervals      The popularity of the last topic in subsequent intervals

According to the proposed Equation 3, the feature vector of countries is derived from the set of the ten topics' popularities during the 12 two-month periods. Next, the modeled data set is accumulated as a matrix in which each country represents a row. In this case study, the dataset contains the feature vectors of 32 countries, and its dimensions are  $32 \times 120$ , as below:

$$\text{Dataset} = \begin{bmatrix} \text{Feature vector of the first country} \\ \text{Feature vector of the second country} \\ \vdots \\ \text{Feature vector of the 32nd country} \end{bmatrix}_{32 \times 120} \quad (4)$$

### 3.3. Clustering

In order to apply machine learning methods to big high-dimensional datasets, we need to perform dimensionality reduction. In high-dimensional datasets, the presence of numerous metadata and features per data item can make it difficult and time-consuming to identify the appropriate features. Furthermore, the computational complexity in high dimensions presents a significant challenge in training machine learning methods, particularly for traditional approaches. This complexity may lead to time-consuming and difficult training processes, potentially hindering the proper functioning of machine learning methods. Consequently, these methods may exhibit a high error rate and low accuracy.

As numerous techniques have been proposed for dimensionality reduction, our aim is to identify the most effective methods for mapping high-dimensional datasets to lower dimensions in this subject. Specifically, we seek suitable dimensionality reduction approaches for datasets that exhibit significant scattering in higher dimensions.

To address this, we utilize two non-linear dimensionality reduction methods: t-SNE [10] and UMAP [27]. These techniques excel in handling sparsely distributed data in high-dimensional spaces [28]. They achieve dimensionality reduction by projecting the data into a new space while preserving the relative distances between the data points [28]. In essence, they provide a compressed representation of the high-dimensional space while maintaining the proximity and distances between the data points. t-SNE

and UMAP are commonly employed in textual data analysis and similar applications for dimension reduction [28].

Besides, since the data in this study is unlabeled, clustering is employed to group objects in the dataset and form meaningful clusters [29]. Multiple clustering algorithms exist, each with unique properties and characteristics, aiming to ensure similarity within clusters and distinctiveness between them. This case study focuses on three traditional clustering algorithms: K-Means [30], FCM [11], and Hierarchical Clustering (HC) [31], which are among the most widely used and effective clustering algorithms [32]. K-Means partitions data into clusters based on similarity and iteratively optimizes the cluster center weights. K-means is a simple and efficient method widely used in various domains due to its scalability, interpretability, and capability to produce clear clusters [32]. FCM, a fuzzy variant of K-Means, is effective for clustering noisy data by assigning data points to clusters based on their weights and iteratively optimizing the cluster center weights. FCM offers soft clustering, accommodating multiple cluster memberships and noise robustness [32]. HC utilizes hierarchical clustering to divide data into smaller clusters, recursively, generating the entire cluster hierarchy. HC generates a hierarchical structure, allowing for cluster interpretation without prior knowledge of cluster numbers. It provides visual representations of cluster relationships and similarities at different levels [33].

The study applies these three clustering methods to countries with and without reducing the dataset's dimensions. It enables obtaining high-level and analyzable information, facilitating the comparison among similar countries. By employing two dimension-reducing methods (as well as one none-reducing method) and three clustering methods, the study generates nine model pairs. The determination of the best methods will be discussed later in the paper.

### 3.4. Selecting the dimension reduction and clustering pair

In order to select the optimal dimension reduction and clustering methods, we employ four key clustering criteria: Davies–Bouldin index (DBI) [6], Silhouette Coefficient (SC) [7], Calinski-Harabasz index (CHI) [8], and Dunn Index [9]. These criteria are widely recognized for their effectiveness in revealing the underlying clustering structure within a dataset [34]. By evaluating them, we can determine the most suitable dimension reduction and clustering techniques for our study.

Davies–Bouldin index [6] is a clustering evaluation metric used to assess the quality of data partitioning into clusters. The calculation involves considering the distance between cluster centers and the internal variance of the clusters. This measure computes the distance between the center of each cluster and the centers of other clusters. It then divides this distance by the sum of the internal variance of that cluster. Subsequently, the ratio is computed for each cluster. This measure is equivalent to the mean of these ratios. It quantifies the average maximum ratio of dispersion within clusters to dispersion between clusters. It evaluates the output value for the number of clusters and identifies the clustering algorithm that maximizes inter-cluster distance and minimizes intra-cluster distance. A lower DBI value indicates better clustering performance. Dunn Index (DI) [9] is a clustering evaluation criterion that quantifies the clustering quality. This measure assesses clustering quality by quantifying the distance between points within a cluster and points between clusters. It is calculated by dividing the smallest distance between any two cluster centroids (known as the lowest inter-cluster distance) by the largest distance between any two points within any cluster (known as the highest intra-cluster distance). A higher DI value indicates better clustering performance. The Silhouette Coefficient (SC) [7] is a clustering evaluation criterion that assesses clustering quality by quantifying the distances between points within a cluster and the distances between points in neighboring clusters. It is calculated as the mean difference between the distance of a point from all points within its own cluster and the distance from all points in neighboring clusters, divided by the larger of these two distances. A higher coefficient of this measure indicates superior performance. Finally, Calinski-Harabasz index (CHI) [8] is based on the ratio of the inter-cluster variance to intra-cluster variance. The clustering quality is better when the inter-cluster variance is larger and the intra-cluster variance is smaller. Moreover, the clustering is superior, the

higher the CHI index value. Based on the preceding sub-section, nine established cases are available for selecting the dimensionality reduction and clustering methods. However, determining the most suitable methods poses a challenge. Two approaches, visual and numerical, are proposed to aid in selecting the appropriate methods. To this end, the evaluation criteria, including CHI, SC, DBI, and DI, are calculated for all cases. Then, each criterion's lowest and highest values across all cases determine the interval for that measure. Next, each of the four criteria's interval is divided into four equal sub-intervals by introducing three thresholds. In Table 1, the threshold values are denoted as Good, Normal, and Bad. The interval is specified by best and worst values.

Table 1 Threshold values for evaluation criteria

Best	Good	Normal	Bad	Worst	Threshold Metric
26.7434	20.1787	13.6141	7.0495	0.4849	CHI
0.3443	-0.0459	-0.4361	-0.8263	-1.2165	SC
0.7357	2.4933	4.2509	6.0084	7.7660	DBI
0.00058	0.00046	0.00035	0.00023	0.00012	DI

The visual method uses four gray-scale colors for the four sub-intervals of each criterion, with the best mode being the darker color and the worst state being the lighter color. Further discussion is provided in the next section.

In the numerical method, the criteria's values are scaled between zero and one hundred to facilitate an accurate examination. The scaled value is calculated as follows:

$$X_{\text{new}} = \frac{(x - x_{\min})}{(x_{\max} - x_{\min})} \quad (5)$$

$x_{\min}$  is the lowest interval value,  $x_{\max}$  is the largest value of the considered evaluation criterion, and the symbol  $x$  represents the value of the criterion. This normalization is accomplished by ensuring that the best value of an interval is represented as 100 while the worst value is 0. As for the DBI criterion, a lower value is preferable; its scaled value is subtracted from one hundred. Afterward, the criteria's normalized values of each feature reduction and clustering pair are averaged. Finally, by comparing the averaged values of different methods, the optimal clustering, dimension reduction, as well as cluster number will be determined.

#### 4. Experiment

The main part of the implementations has been done in the Python programming environment on Windows 10, 64-bit. The hardware was a computer with corei5, 3.4 GHz frequency, and 6 megabytes of level three (L3) cache memory processor, 4 GB of RAM, and 2 GB of graphics card. The dataset used includes 14 million tweets related to the Covid-19 virus from the years 2020 and 2021. In order to normalize, 120,000 tweets have been randomly selected for each two-month period. Finally, the dataset containing 1,440,000 tweets for 12 two-month time periods has been used. To tag the location of tweets related to each country, the common natural language processing framework GATE has been used [3]. This framework includes various tools that are used to process and analyze text, identify and categorize information, extract information, and produce various outputs such as reports and charts. In order to pre-process tweets, the required functions were called from the Gensim library, which is one of the most famous libraries used in topic modeling [3].

At first, we present the experiments for extracting static topics without considering the time factor. Subsequently, the topics are dynamically evaluated, taking into account the temporal aspect. Finally,

the proposed method is compared with previous works. The case study is performed for countries that have sufficient tweets in the dataset.

#### 4.1. Static topics

Topics are initially investigated regardless of time. Table 2 shows the three hottest topics for each country. The Vaccine has been the leading topic for nearly all countries, as indicated in the table. Work & telecommuting has emerged as the second topic in most countries. The top three topics exhibit a consistent trend across most of the countries, indicating a similar tendency among them. Figure 3 illustrates the worldwide distribution of topics based on the global percentage of tweets. Among these topics, Vaccine exhibits the highest percentage, while Work & telecommuting and Masking rank second and third, respectively.

Table 2 Hottest topics per country. Numbers 1, 2, and 3 represent the first, second, and third hot topics, respectively.

Country \ Topic	Spread	Work & telecommuting	Students and education	Vaccine	Power & politics	Economy	Voluntary affairs	Plasma	Cases & death cases	Masking
USA		3		1						2
India	3			1					2	
China				1	2		3			
Australia	2			1					3	
UK	2			1	3					
Canada	2			1						3
Pakistan				1	3				2	
Japan				1		3			2	
Germany				1					2	3
France		2		1					3	
Ireland		2		1					3	
Singapore		2		1						3
UAE		2		1					3	
Mexico		3		1					2	
Italy		2		1					3	
Sweden				1		3			2	
Brazil		3		2					1	
Iran	2			3					1	
Russia		3		1			2			
South Korea		3		1						2
Spain		3		1					2	
Switzerland		2		1						3
Turkey		3		1					2	
Netherlands		2		1	3					
Belgium		2		1					3	
Denmark				1	3					2
Chile		3		1					2	
Saudi Arabia	3	2		1						
Peru		3		1					2	
Portugal		2		1					3	
Qatar		2		1	3					2
Ecuador		2		1					3	

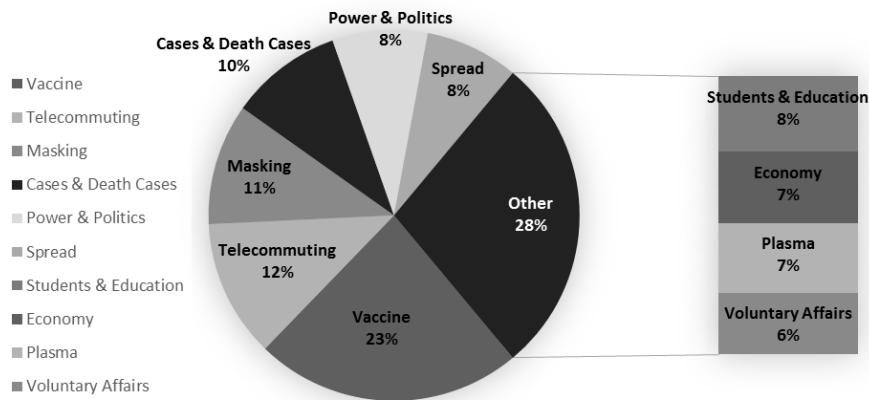


Figure 3 Percentage of topics in the dataset.

## 4.2. Dynamic topics

Table 2 indicates that the USA and South Korea have exhibited similar behavior. However, when we look at the details (i.e., the trend of the topics as shown in Figure 4), we can see that their topics exhibit dissimilar trends. In Figure 4, the trends of these topics vary significantly between the two countries. As such, a dynamic analysis of topics is required. This subsection examines the influence of the time factor. The popularity of topics ( $p_k(t)$ ) values for the entire world are presented in Table 3. Vaccine, Work & telecommuting, and Masking are the most popular topics on a global scale. Figure 5 illustrates the popularity trend of these topics worldwide.

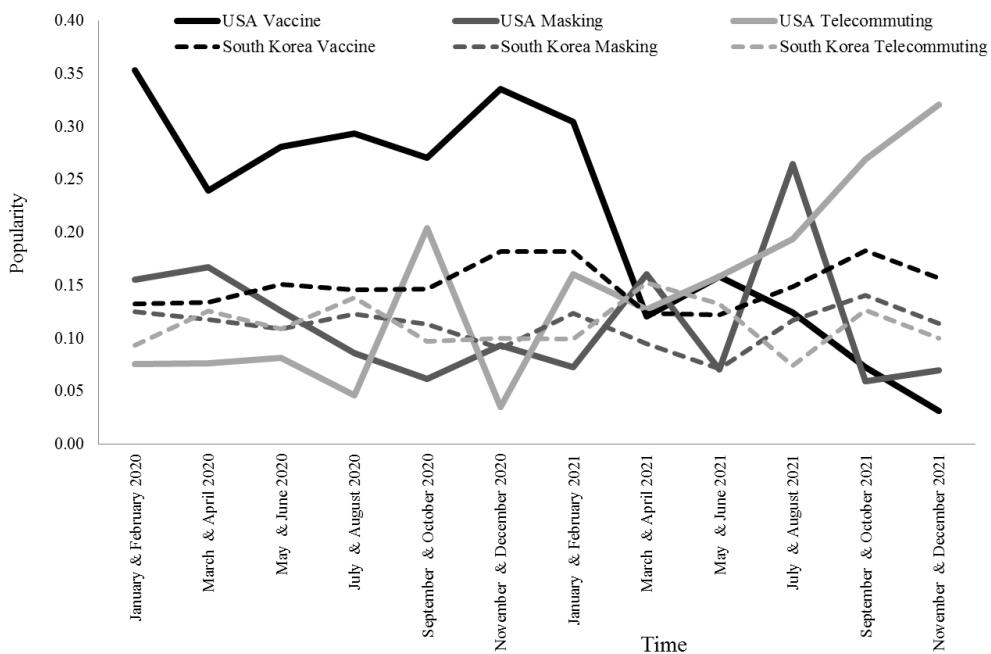


Figure 4 Topics popularity trends in South Korea & the USA.

Table 3 The popularity of topics in the world

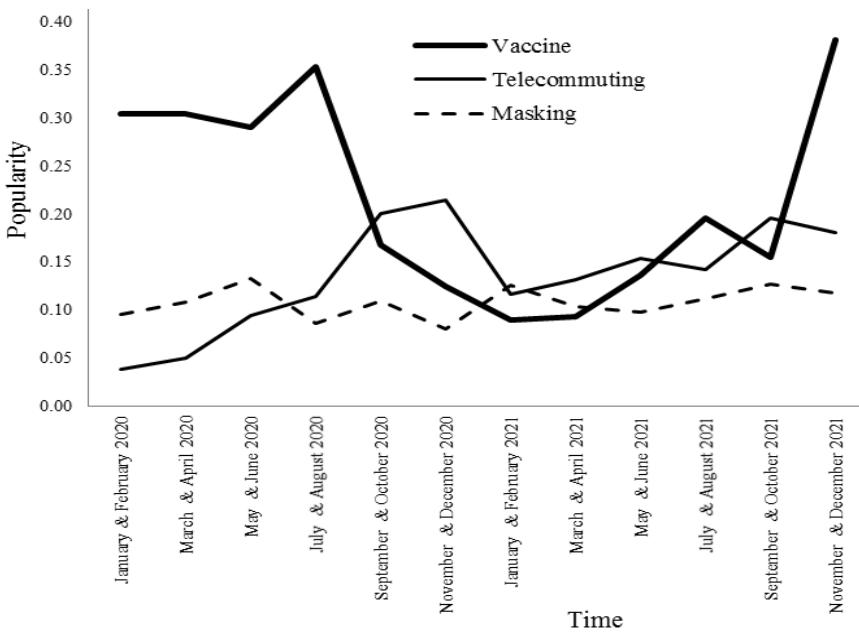


Figure 5 The popularity of topics in the world.

Tables 4 to 6 show the popularity of topics in the three countries with the highest tweet volume, including the USA, India, and China. The topics in topic popularity tables are arranged in descending order based on their  $P_k$  values. Appendix 1 presents the topic popularity tables for other countries, including Australia, the UK, Canada, Pakistan, Japan, Germany, France, Ireland, Singapore, UAE,

Mexico, Italy, Sweden, Brazil, Iran, Russia, South Korea, Spain, Switzerland, Turkey, Netherlands, Belgium, Denmark, Chile, Saudi Arabia, Peru, Portugal, and Qatar.

Table 4 The popularity of topics in USA.

Table 5 The popularity of topics in India.

Table 6 The popularity of topics in China.

		2020						2021							
		Topic													
Students	Vaccine	0.0196	0.0635	0.0929	0.1000	0.1470	0.1343	0.1593	0.0710	0.1582	0.0538	P January & February			P <sub>K</sub>
	Politics	0.0109	0.0985	0.0832	0.1094	0.1572	0.0995	0.0862	0.1285	0.1433	0.0828	P March & April			
	voluntarily	0.0686	0.1292	0.1205	0.0786	0.1184	0.1165	0.1283	0.1162	0.0819	0.0413	P May & June			
	Masking	0.0430	0.0847	0.1291	0.1283	0.1933	0.0622	0.1085	0.1285	0.0817	0.0405	P July & August			
	Economy	0.1241	0.039	0.1119	0.1414	0.1516	0.1034	0.0922	0.0846	0.0925	0.0593	P September & October			
	Spread	0.1256	0.0821	0.0823	0.0908	0.0651	0.0864	0.1016	0.1405	0.1334	0.0917	P November & December			
	Telecommuting	0.1237	0.1240	0.0904	0.1156	0.0626	0.1114	0.0341	0.0935	0.1273	0.1143	P January & February			
	Plasma	0.1213	0.1333	0.0955	0.0650	0.0432	0.0964	0.0424	0.0923	0.1265	0.1834	P March & April			
	Death	0.1313	0.0757	0.0637	0.0551	0.0229	0.1018	0.0919	0.1482	0.0580	0.251	P May & June			
		0.1443	0.1046	0.0886	0.0732	0.0252	0.0814	0.1484	0.0404	0.0404	0.2530	P July & August			
		0.1782	0.1140	0.0805	0.1134	0.0286	0.0413	0.1899	0.0609	0.0887	0.1039	P September & October			
		0.2197	0.1228	0.1216	0.0780	0.0578	0.1238	0.1124	0.0540	0.0237	0.0859	P November & December			
													1.3614	1.3109	
													1.2956	1.1718	
													1.1610	1.1605	
													1.1590	1.1561	
													1.1493	1.0735	

Figure 6 illustrates the trend of hot topics in the USA, India, and China. Appendix 2 shows the trend of hot topics for other countries, including Australia, United Kingdom (UK), Canada, Pakistan, Japan, Germany, France, Ireland, Singapore, UAE, Mexico, Italy, Sweden, Brazil, Iran, Russia, South Korea, Spain, Switzerland, Turkey, Netherlands, Belgium, Denmark, Chile, Saudi Arabia, Peru, Portugal, and Qatar.

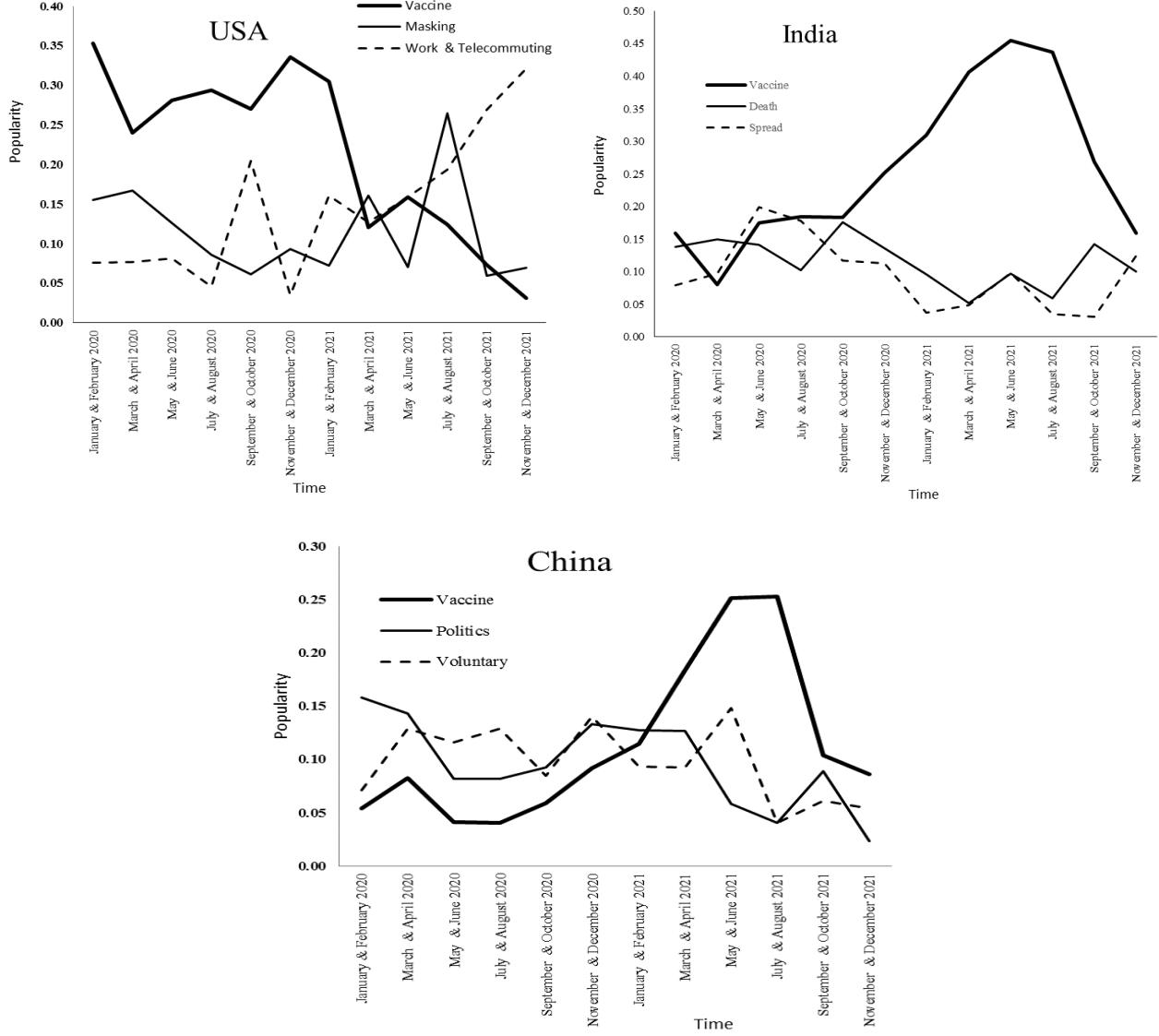


Figure 6 Popularity trend of topics of 3 countries.

#### 4.3. Evaluation

Figure 7 compares the performances of the three clustering methods K-Means, FCM, and HC, before and after dimension reduction using UMAP and t-SNE in terms of the discussed clustering criteria (CHI, SC, DBI, and DI). Besides, seven different cluster numbers (3 to 9 clusters) are evaluated. Each row in the table corresponds to one of these criteria, while each column represents a specific cluster number ( $k$ ) value. By visually inspecting, the FCM clustering and the UMAP dimension reduction methods (Figure 7b) result in the darkest colors.

After selecting the FCM clustering and UMAP dimension reduction methods, we look for the darkest column to determine the number of clusters. The leftmost column, i.e., three clusters, is clearly the

darkest and therefore selected. It is also the darkest column in the figure. Table 7 presents the numerical verification of the values following the visual approach. It contains rows with CHI, SC, DBI, and DI evaluation criteria values, which have been normalized using Equation 5. The average of normalized criteria for each state is provided at the end of the columns. Numerical analysis confirms that the FCM clustering method achieves its highest average value for three clusters when combined with the UMAP dimension-reduction technique. The clustering results are as follows.

- Russia, Netherlands, France, Spain, Switzerland, UK, Peru, and Portugal.
- USA, Australia, Belgium, Canada, Pakistan, Japan, Germany, Ireland, UAE, Italy, Denmark, Chile, and Qatar.
- India, China, Singapore, Mexico, Sweden, Brazil, Iran, South Korea, Turkey, and Saudi Arabia.

K-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index		4.1457	3.3999	3.2775	2.9555	2.7696	2.7357	2.6998
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index		0.00035	0.00038	0.00034	0.00023	0.00021	0.0002	0.00019
Fuzzy C-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index		4.8578	2.5538	2.8792	3.1532	2.9311	2.5595	2.3553
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index			0.00045		0.000309	0.00037	0.00023	0.0002
Hierarchical clustering		3	4	5	6	7	8	9
Calinski-Harabasz Index		4.0744	3.5842	3.4098	3.2431	3.1339	3.076	3.0354
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index		0.00044	0.00043	0.00041		0.00031	0.00036	0.00027

K-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index				13.1283	17.5486	17.1341	16.0354	
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index		0.00037	0.00039	0.00033	0.00028	0.00022	0.00024	0.00012
Fuzzy C-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index		14.2934	10.0632	14.2934	14.2934	15.0493	8.0979	
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index			0.00041	0.00043	0.00034	0.0003		
Hierarchical clustering		3	4	5	6	7	8	9
Calinski-Harabasz Index		16.536	11.1271	16.5316	14.7389	12.5156	11.5004	11.207
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index			0.00042	0.00043	0.0004			

K-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index								19.0647
Silhouette coefficient								
Davies-Bouldin Index								
Dunn Index		0.0004	0.00043	0.00038	0.00037	0.00022		
Fuzzy C-Means		3	4	5	6	7	8	9
Calinski-Harabasz Index		2.4391	1.4377	1.7468	1.2995	1.2227	1.4377	1.3797
Silhouette coefficient		-0.2165	-0.1373	-1.2165	-0.2165	-0.2165	-0.2967	
Davies-Bouldin Index		2.728455	2.890971	4.219782	5.2779478	4.123216	5.277948	
Dunn Index		0.00034	0.00025	0.00033	0.00024	0.00027	0.00026	0.00017
Hierarchical clustering		3	4	5	6	7	8	9
Calinski-Harabasz Index		0.4843	1.4171	1.5901	1.8158	1.4832	1.2678	1.0729
Silhouette coefficient			-0.09	-0.1605	-0.1736	-0.215	-0.2331	-0.3465
Davies-Bouldin Index		7.766076	6.781978	6.377904	7.4292536	6.307828	4.657593	3.950288
Dunn Index		0.00041	0.000408	0.00035	0.00034	0.00023	0.00021	0.00012

(b)

(c)

Figure 7 Visual selection of dimension reduction and clustering methods as well as number of clusters. (a) Without dimension reduction. (b) Dimension reduction with UMAP (c) Dimension reduction with t-SNE

Table 7 Normalized values of evaluation criteria, for K-Means, FCM, and HC clustering methods, before dimension reduction and after dimension reduction with UMAP and t-SNE and for varying numbers of clusters

K-Means	Clustering method	Evaluation criteria	Without dimension reduction		Dimension reduction with UMAP		Dimension reduction with t-SNE				
			Number of clusters (Sorted according to performance)								
			4	3	5	6	7	8	9	4	3
CHI	K-Means	0.5652	0.8213	0.8328	0.111	0.5435	0.9569	1	0.8179	0.8696	0.9819
		0.5	0.8043	0.8388	0.1394	0.4565	0.9578	0.9915	0.7977	0.8478	0.9789
		0.4783	0.8233	0.8323	0.1064	0.3478	0.9592	0.9525	0.71	0.6739	0.9931
		0.2391	0.8699	0.8175	0.0941	0.2174	0.9591	0.962	0.6498	0.5652	1
SC	K-Means	0.1957	0.8837	0.815	0.087	0.2609	0.9477	0.9115	0.6363	0.6087	0.9791
		0.1739	0.9007	0.8128	0.0857	0	0.9693	0.9189	0.5922	0.5435	0.9962
		0.1522	0.9163	0.8076	0.0843	0	0.9693	0.9189	0.5922	0.2174	0.9857
		0.587	0.9607	0.9904	0.8851	0	0.9693	0.9189	0.5922	0.2174	0.98988
DBI	K-Means	0.5652	0.8213	0.8328	0.111	0.5435	0.9569	1	0.8179	0.8696	0.9819
		0.5	0.8043	0.8388	0.1394	0.4565	0.9578	0.9915	0.7977	0.8478	0.9789
		0.4783	0.8233	0.8323	0.1064	0.3478	0.9592	0.9525	0.71	0.6739	0.9931
		0.2391	0.8699	0.8175	0.0941	0.2174	0.9591	0.962	0.6498	0.5652	1
DI	K-Means	0.1957	0.8837	0.815	0.087	0.2609	0.9477	0.9115	0.6363	0.6087	0.9791
		0.1739	0.9007	0.8128	0.0857	0	0.9693	0.9189	0.5922	0.5435	0.9962
		0.1522	0.9163	0.8076	0.0843	0	0.9693	0.9189	0.5922	0.2174	0.9857
		0.587	0.9607	0.9904	0.8851	0	0.9693	0.9189	0.5922	0.2174	0.98988

Method		FCM									Mean	
		Number of clusters (Sorted according to performance)										
		CHI	SC	DBI	DI	Mean	CHI	SC	DBI	DI		
HC		0.6357	0.7826	0.8331	0.8217	0.1053	0.6533	0.8283	0.7716	0.8468	0.1665	<b>0.5826</b>
		0.615	0.6957	0.7947	0.833	0.1367	0.6426	0.913	0.7664	0.7999	0.0912	0.5706
		0.6107	0.6739	0.8245	0.8264	0.118	0.6224	0.7174	0.8465	0.8468	0.0788	0.5601
		0.5959	0.6304	0.8116	0.8259	0.1114	0.5454	0.4109	0.8662	0.803	0.1016	0.5052
		0.583	0.5217	0.8857	0.8253	0.0987	0.539	0.5435	0.7635	0.7519	0.0954	0.495
		0.554	0.413	0.8785	0.8243	0.1009	0.485	0.2391	0.82	0.7999	0.079	0.493
		0.5401	0.3261	0.9091	0.8281	0.0971	0.4729	0.1739	0.8465	0.7999	0.0712	0.4901
		<b>0.8774</b>	1	0.9423	0.9561	0.6113	<b>0.9419</b>	0.913	0.9272	0.9272	1	<b>0.856</b>
		0.822	0.8478	0.9148	0.9111	0.6134	0.818	0.9348	0.9766	0.8348	0.5259	0.8296
		0.805	0.8696	0.9167	0.8885	0.5451	0.783	1	0.9304	0.8348	0.3648	0.801
		0.736	0.7826	0.889	0.8681	0.4053	0.7663	0.6739	0.9766	0.8887	0.5259	0.7424
		0.733	0.6522	0.9659	0.8555	0.4582	0.7531	0.6304	0.98	0.8762	0.5259	0.6971
		0.718	0.6739	0.9561	0.8228	0.4195	0.711	0.4783	0.9757	0.8348	0.5546	0.689
		0.694	0.6087	0.9627	0.7976	0.4083	0.623	0.3913	0.9766	0.8348	0.2899	0.62
		<b>0.3802</b>	0.6261	0.14	0.7192	0.0355	<b>0.4781</b>	0.4783	0.7166	0.6407	0.0767	<b>0.9103</b>
		0.3457	0.6304	0	0.7523	0	0.429	0.1087	0.7427	0.8298	0.0341	0.9
		0.333	0.5	0.1121	0.6766	0.0421	0.4259	0.2826	0.6934	0.6914	0.0363	0.8572
		0.323	0.1957	0.4422	0.6262	0.0298	0.378	0.3261	0.5182	0.6407	0.0281	0.8336
		0.3113	0.4783	0.0479	0.6682	0.0507	0.322	0.2609	0.3539	0.6407	0.031	0.835
		0.282	0.2391	0.2074	0.6417	0.038	0.321	0.3043	0.3539	0.5893	0.0363	0.829
		0.281	0	0.5428	0.5574	0.0224	0.3216	0.4565	0.5044	0	0.0481	0.702

This research focuses on analyzing the output of topic modeling through clustering. Previously, Palanichamy et al. [4], Sun and Yin [2], and Xie et al. [5] have conducted static analyses on the output of topic modeling. They have utilized static clustering of topics using the Euclidean [4] and JSD [2, 5] methods. Sun and Yin [2] and Xie et al. [5] have employed a similar method. A comparison is made in Table 8 in terms of the evaluation criteria, including CHI, SC, DBI, and DI. It should be noted that higher values of CHI, SC, and DI and lower values of DBI are preferable. Consequently, in all criteria, the proposed method has achieved the best performance among all available methods.

Table 8 Comparison of the proposed method with close work

Method	Evaluation metric	CHI	SC	DBI	DI
The proposed method	22.0782	0.2931	0.7623	0.0003	
Y. Palanichamy et al [4]	15.9772	0.1848	0.9517	0.0001	
L. Sun and Y. Yin [2] & Y. Xie et al. [5]	20.1023	0.2149	0.8347	0.0003	

As the proposed method focuses on the dynamic analysis of topics, a feature vector has been proposed to capture topic changes over time. Besides, selecting the optimal clustering and dimension reduction methods and clusters number resulted in the outperformance over previous methods.

## 5. Conclusion

Analyzing the time-dependent dynamics of topic modeling outputs using machine learning methods poses significant challenges. As such, the topic popularity over time metric has been proposed, which is derived from the topic modeling outputs. Subsequently, this metric was used to model the feature vector for each entity (country) over time. Selecting the appropriate dimension reduction method and corresponding clustering algorithm was performed by identifying the best values of evaluation criteria, both visually and numerically. Finally, the proposed method has demonstrated superior performance over similar methods in terms of all evaluation criteria.

Based on the static analysis of the results, the Vaccine, Work and telecommuting, and Masking emerged as the first three topics of discussion across all countries during the years 2020 and 2021. While the topics discussed were similar across all countries, the proposed method revealed variations in the trends of these topics among different countries. As a result, the countries with similar top three topics were grouped into different clusters after dynamic clustering. Indeed, leveraging the dynamic analysis of topic modeling outputs in relation to various entities can contribute to a more comprehensive understanding of time-based topic changes. The proposed method can facilitate the analysis of entity dynamics across domains such as medicine, Politics, and psychology in natural language processing research, leading to improved research outcomes. This study solely examined the clustering of entities within the topic modeling output. Future research can explore the utilization of other machine learning methods, such as regression and classification. Finally, we proposed an indirect text clustering methodology that converts text clustering to traditional machine learning clustering. In this regard, a fundamental question arises: Is it better to cluster the texts directly as in the previous research or extract the parameters using heuristic methods and then cluster based on them (like the approach we used in this paper)? Investigating this problem is an interesting fundamental future research.

## Statements and Declarations

### Competing interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

### Ethical Approval

Not applicable

### Authors contribution

Faezeh Azizi: Methodology, Software, Original draft preparation

Hamed Vahdat-Nejad: -Supervision- Conceptualization, Methodology- Reviewing and Editing

Hamideh Hajiabadi: Supervision- Reviewing and Editing

### Code and data availability

<https://github.com/FaezehAzizi1995/Paper3.git>

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Appendices

## Appendix 1

Table 9 Popularity of topics in Australia

Topic	2020				2021				$P_K$				
	0.30137	$P_{January \& February}$	0.327181	$P_{March \& April}$	0.30853881	$P_{May \& June}$	0.2652744	$P_{July \& August}$	0.16662	$P_{September \& October}$	0.28653	$P_{November \& December}$	
Vaccine	0.295056	$P_{January \& February}$	0.311067	$P_{March \& April}$	0.33012	$P_{May \& June}$	0.094595	$P_{July \& August}$	0.21479	$P_{September \& October}$	3.245764408	$P_{November \& December}$	

		Telecommuting				
		Death				
		Politics				
		Masking				
		Economy				
		Spread				
		Plasma				
		Students				
	voluntarily					
0.0400959	0.054696	0.0684245	0.10438	0.0758335	0.0544781	0.1048159
0.052086	0.039444	0.070544	0.113527	0.067762	0.067509	0.090771
0.0604076	0.0465793	0.0412421	0.1055313	0.0749636	0.0982533	0.0803008
0.0542102	0.0637636	0.0428794	0.1021995	0.0675405	0.102866	0.1139747
0.08931	0.06985	0.07731	0.12983	0.07785	0.09891	0.08824
0.08868	0.05769	0.05435	0.09511	0.05721	0.07104	0.09178
0.03001	0.07305	0.07814	0.08862	0.0722	0.06738	0.05125
0.043461	0.064593	0.072169	0.088517	0.070574	0.075359	0.060606
0.082752	0.034895	0.046859	0.093719	0.075274	0.059821	0.076271
0.06172	0.04247	0.03681	0.06512	0.05436	0.04134	0.05436
0.059966	0.061655	0.043074	0.081926	0.096284	0.057432	0.040541
0.07306	0.04225	0.05106	0.08803	0.07835	0.03433	0.02993
						0.88283485
						0.868191256
						0.828713873
						0.682860899
						0.650931288
						1.156509995
						1.425665237
						1.52276709

Table 10 Popularity of topics in UK

Topic	2020		2021		$P_K$
	Vaccine	Telecommuting	Politics	Telecommuting	
0.1152	0.0309	0.2665	$p_{\text{January \& February}}$		
0.1193	0.1199	0.2194	$p_{\text{March \& April}}$		
0.1108	0.0963	0.3146	$p_{\text{May \& June}}$		
0.1419	0.1863	0.1581	$p_{\text{July \& August}}$		
0.0963	0.1815	0.1486	$p_{\text{September \& October}}$		
0.1228	0.0961	0.2947	$p_{\text{November \& December}}$		
0.1217	0.1688	0.3238	$p_{\text{January \& February}}$		
0.1431	0.2060	0.1111	$p_{\text{March \& April}}$		
0.0791	0.1152	0.1837	$p_{\text{May \& June}}$		
0.1096	0.0648	0.1974	$p_{\text{July \& August}}$		
0.1180	0.0650	0.0915	$p_{\text{September \& October}}$		
0.1045	0.1337	0.1120	$p_{\text{November \& December}}$		
				2.421993573	
				1.465153255	
				1.403445717	

Table 11 Popularity of topics in Canada

Economy						
voluntarily						

Table 12 Popularity of topics in Pakistan

Topic		2020			2021							
		P January & February	P March & April	P May & June	P July & August	P September & October	P November & December					
Vaccine		0.0480	0.0150	0.0420	0.0945	0.0780	0.1096	0.1111	0.1246	0.1561	0.2207	P January & February
Death		0.0666	0.0456	0.0333	0.1070	0.0842	0.1087	0.1175	0.0789	0.1350	0.2227	P March & April
Politics		0.0432	0.0467	0.0380	0.0692	0.0951	0.0882	0.1366	0.0640	0.1470	0.2716	P May & June
Masking		0.0477	0.0614	0.0307	0.0631	0.0904	0.1109	0.0921	0.0529	0.163	0.2866	P July & August
Telecommuting		0.0559	0.0786	0.0437	0.0769	0.0751	0.0664	0.0664	0.0751	0.1346	0.3269	P September & October
Economy		0.0672	0.0710	0.0654	0.0934	0.0878	0.0542	0.0635	0.0598	0.0803	0.3570	P November & December
Students		0.0594	0.0815	0.0682	0.0748	0.0638	0.0660	0.0859	0.0616	0.0837	0.3543	P January & February
Spread		0.05882	0.06138	0.0920	0.0997	0.0383	0.1202	0.0818	0.0997	0.1074	0.2409	P March & April
Plasma		0.0538	0.0539	0.1736	0.0508	0.0658	0.0868	0.08982	0.1497	0.1107	0.1646	P May & June
Voluntary		0.0648	0.0648	0.1512	0.07099	0.1450	0.04321	0.0679	0.1635	0.0709	0.1574	P July & August
Vaccine		0.0476	0.0539	0.1206	0.0380	0.1556	0.0691	0.06031	0.1269	0.1142	0.2126	P September & October
		0.06019	0.0555	0.1898	0.0601	0.0972	0.1157	0.0925	0.0925	0.0601	0.1759	P November & December
												P_K
												2.9915
												1.3644
												1.1497
												1.0768
												1.0489
												0.8991
												0.6895
												0.673
												0.6081
												0.7209

Table 13 Popularity of topics in Japan

Topic	2020			2021			P_K
	P January & February	P March & April	P May & June	P July & August	P September & October	P November & December	
Vaccine	0.286	0.279	0.304	0.200	0.225	0.366	0.155
	0.212	0.169	0.177	0.109	0.156	0.156	2.643308203

Table 14 Popularity of topics in Germany

Students								
Plasma								
Voluntary								

Table 15 Popularity of topics in France

Topic	2020				2021				$P_K$
	P January & February	P March & April	P May & June	P July & August	P September & October	P November & December	P January & February	P March & April	
Vaccine	0.072380.067020.034850.075060.101870.067020.061660.147450.104550.26809								0.0520.0480.083
Telecommuting	0.060340.054590.040220.071830.074710.066090.068960.123560.140800.29885								0.0640.0400.057
Death	0.048850.052110.068400.048850.097710.091200.068400.107490.153090.26384								0.0760.0300.058
Masking	0.04270.064060.046260.067620.074730.078290.081850.10320.117440.32384								0.0430.0140.046
Spread	0.05970.029850.064680.062190.049750.052240.089550.111940.106970.37313								0.0530.0370.056
Politics	0.068180.068180.094160.081170.087660.071430.094160.087660.133120.21429								0.0530.1070.053
Economy	0.065630.084940.104240.065630.069490.061770.142850.077220.135130.19305								0.0730.1100.110
Students	0.051940.069260.125540.051940.069260.103890.125540.073590.142850.18614								0.0480.1120.118
Plasma	0.047850.06220.105260.114830.047850.129190.153110.086120.138760.11483								0.0420.1200.096
Voluntary	0.100960.115380.028840.139420.06250.139420.1250.067300.100960.12019								0.835149815
	0.040980.069670.020490.069670.118850.147540.102460.032790.069670.32787								0.808835938
									0.690494278

Table 16 Popularity of topics in Ireland

	2020	2021	

		Topic			
	Vaccine				
	Telecommuting				
	Death				
	Masking				
	Politics				
	Spread				
	Plasma				
	Economy				
	Voluntary				
	Students				
0.102	0.102	0.232	p January & February		
0.104	0.135	0.200	p March & April		
0.099	0.164	0.099	p May & June		
0.105	0.115	0.205	p July & August		
0.095	0.146	0.241	p September & October		
0.100	0.215	0.165	p November & December		
0.090	0.131	0.253	p January & February		
0.095	0.145	0.204	p March & April		
0.047	0.094	0.297	p May & June		
0.135	0.113	0.178	p July & August		
0.058	0.112	0.370	p September & October		
0.071	0.184	0.241	p November & December		
				P_K	
					2.837396248
					1.425494297
					1.207514754
					1.194035962
					1.045946785
					1.028200809
					0.840455949
					0.826045722
					0.807146045
					0.787763428

Table 17 Popularity of topics in Singapore

		Topic			
	Vaccine				
	Telecommuting				
	Masking				
0.0493	0.0699	0.0493	0.0823	0.0411	0.1234
0.0669	0.0382	0.0956	0.1004	0.1196	0.1004
0.0563	0.0093	0.0985	0.0985	0.0563	0.0938
0.0598	0.0419	0.0718	0.0718	0.0838	0.0538
					0.840455949
					0.826045722
					0.807146045
					0.787763428
					2.689513459
					1.659680098
					1.106123532

	Death						
	Spread						
	Politics						
	Economy						
	Students						
	Plasma						
	Voluntary						
0.10280	0.09813	0.06542	0.10747	0.10747	0.09345	0.21962	p January & February 0.059 0.078 0.055 0.102 0.094 0.094 0.078
0.06224	0.08713	0.10788	0.07468	0.11618	0.08713	0.24066	p March & April 0.046 0.065 0.046 0.104 0.104 0.104 0.081
0.05909	0.05454	0.09545	0.06818	0.11363	0.09090	0.33181	p May & June 0.049 0.104 0.099 0.104 0.104 0.104 0.049
0.07725	0.06866	0.11587	0.05579	0.06008	0.10729	0.31759	p July & August 0.06 0.07 0.105 0.075 0.07 0.07 0.125
0.06091	0.06091	0.08629	0.07614	0.06599	0.06091	0.32295	p September & October 0.061 0.067 0.117 0.067 0.067 0.067 0.067
0.04911	0.08929	0.08482	0.08036	0.10714	0.0625	0.33036	p November & December 0.055 0.045 0.055 0.091 0.096 0.110 0.064
0.05263	0.0614	0.0614	0.08772	0.09211	0.11404	0.36842	p January & February 0.081 0.022 0.063 0.095 0.095 0.095 0.072
0.10256	0.07692	0.07051	0.07692	0.13461	0.17307	0.12179	p March & April 0.077 0.054 0.05 0.063 0.090 0.095 0.122
0.08433	0.10843	0.08433	0.11445	0.10843	0.12048	0.12048	p May & June 0.099 0.047 0.056 0.056 0.113 0.094 0.094
0.11486	0.13514	0.08784	0.10135	0.06757	0.17568	0.11486	p July & August 0.129 0.059 0.108 0.054 0.054 0.054 0.113
0.13380	0.09154	0.06338	0.09859	0.05633	0.11971	0.13380	p September & October 0.058 0.102 0.058 0.102 0.029 0.024 0.082
0.13821	0.09756	0.06504	0.12195	0.09756	0.17886	0.01626	p November & December 0.051 0.061 0.102 0.051 0.061 0.061 0.112
							2.645636895 1.38406352 1.127135068 1.063634843 1.037821473 1.0296879 0.988267045 0.91813703 0.829307694 0.968283662 0.980958982 0.779918771 0.91813703 1.003142436 1.064934337

Table 18 Popularity of topics in UAE

Topic	2020				2021				$P_K$
	Vaccine	Telecommuting	Death	Spread	Economy	Masking	Politics		
0.10280	0.09813	0.06542	0.10747	0.10747	0.09345	0.21962	p January & February 0.059 0.078 0.055 0.102 0.094 0.094 0.078		
0.06224	0.08713	0.10788	0.07468	0.11618	0.08713	0.24066	p March & April 0.046 0.065 0.046 0.104 0.104 0.104 0.081		
0.05909	0.05454	0.09545	0.06818	0.11363	0.09090	0.33181	p May & June 0.049 0.104 0.099 0.104 0.104 0.104 0.049		
0.07725	0.06866	0.11587	0.05579	0.06008	0.10729	0.31759	p July & August 0.06 0.07 0.105 0.075 0.07 0.07 0.125		
0.06091	0.06091	0.08629	0.07614	0.06599	0.06091	0.32295	p September & October 0.061 0.067 0.117 0.067 0.067 0.067 0.067		
0.04911	0.08929	0.08482	0.08036	0.10714	0.0625	0.33036	p November & December 0.055 0.045 0.055 0.091 0.096 0.110 0.064		
0.05263	0.0614	0.0614	0.08772	0.09211	0.11404	0.36842	p January & February 0.081 0.022 0.063 0.095 0.095 0.095 0.072		
0.10256	0.07692	0.07051	0.07692	0.13461	0.17307	0.12179	p March & April 0.077 0.054 0.05 0.063 0.090 0.095 0.122		
0.08433	0.10843	0.08433	0.11445	0.10843	0.12048	0.12048	p May & June 0.099 0.047 0.056 0.056 0.113 0.094 0.094		
0.11486	0.13514	0.08784	0.10135	0.06757	0.17568	0.11486	p July & August 0.129 0.059 0.108 0.054 0.054 0.054 0.113		
0.13380	0.09154	0.06338	0.09859	0.05633	0.11971	0.13380	p September & October 0.058 0.102 0.058 0.102 0.029 0.024 0.082		
0.13821	0.09756	0.06504	0.12195	0.09756	0.17886	0.01626	p November & December 0.051 0.061 0.102 0.051 0.061 0.061 0.112		
								2.645636895 1.38406352 1.127135068 1.063634843 1.037821473 1.0296879 0.988267045 0.91813703 0.829307694 0.968283662 0.980958982 0.779918771 0.91813703 1.003142436 1.064934337	

	Students						
	Voluntary						
	Plasma						

Table 19 Popularity of topics in Mexico

	Topic	2020				2021				$P_K$
		Vaccine	Death	Masking	Telecommuting	Spread	Politics	Economy	Voluntary	
0.0677	0.0847	0.0805	0.0466	0.0889	0.0466	0.0805	0.1271	0.1694	0.2076	p January & February
0.0439	0.0926	0.0829	0.0487	0.0878	0.1024	0.0975	0.1658	0.1121	0.1658	p March & April
0.0506	0.0548	0.0675	0.0886	0.0928	0.0928	0.0801	0.1012	0.2742	0.0970	p May & June
0.0607	0.0769	0.0607	0.0485	0.0607	0.0809	0.0971	0.1214	0.2510	0.1417	p July & August
0.0871	0.0871	0.0746	0.0829	0.0539	0.0663	0.0788	0.1161	0.2323	0.1203	p September & October
0.0631	0.1052	0.0736	0.0947	0.0578	0.0526	0.0894	0.1263	0.2157	0.1210	p November & December
0.0476	0.0654	0.0773	0.0714	0.0535	0.0892	0.1190	0.1190	0.1547	0.2023	p January & February
0.0588	0.0823	0.0529	0.0588	0.0764	0.0705	0.1529	0.1470	0.1	0.2	p March & April
0.1016	0.0593	0.0847	0.0423	0.0847	0.0847	0.1610	0.1271	0.1016	0.1525	p May & June
0.0896	0.0275	0.0827	0.0827	0.0758	0.1448	0.1724	0.0965	0.0620	0.1655	p July & August
0.0780	0.0141	0.0283	0.1134	0.1276	0.1276	0.1418	0.0780	0.0212	0.2695	p September & October
0.0794	0.0198	0.0529	0.1390	0.0993	0.0794	0.1655	0.0397	0.0331	0.2913	p November & December
										2.134947019
										1.728029979
										1.4365425
										1.365720072
										1.03844655
										0.959827495
										0.91823727
										0.828632577
										0.819223044
										0.770393494

Table 20 Popularity of topics in Italy

	2020	2021	

Topic								
	Vaccine	Telecommuting			Death			P <sub>K</sub>
	Masking	Spread			Politics			P <sub>K</sub>
	Economy	P <sub>January &amp; February</sub>			P <sub>May &amp; June</sub>			P <sub>January &amp; February</sub>
	Students	P <sub>March &amp; April</sub>			P <sub>July &amp; August</sub>			P <sub>March &amp; April</sub>
	Voluntary	P <sub>September &amp; October</sub>			P <sub>September &amp; October</sub>			P <sub>May &amp; June</sub>
	Plasma	P <sub>November &amp; December</sub>			P <sub>January &amp; February</sub>			P <sub>July &amp; August</sub>
0.059	0.068	0.077	0.027	0.072	0.059	0.095	0.086	0.168
0.068	0.064	0.064	0.049	0.044	0.054	0.103	0.098	0.226
0.048	0.048	0.086	0.033	0.057	0.057	0.057	0.091	0.227
0.049	0.034	0.049	0.053	0.073	0.053	0.078	0.117	0.137
0.032	0.059	0.070	0.103	0.065	0.065	0.065	0.119	0.130
0.020	0.089	0.083	0.094	0.068	0.083	0.104	0.089	0.109
0.035	0.094	0.041	0.076	0.065	0.053	0.082	0.118	0.136
0.073	0.058	0.080	0.102	0.088	0.088	0.088	0.191	0.095
0.048	0.027	0.062	0.125	0.076	0.104	0.125	0.132	0.160
0.074	0.040	0.054	0.067	0.081	0.094	0.135	0.168	0.087
0.052	0.120	0.141	0.188	0.188	0.188	0.188	0.195	0.195
0.057	0.136	0.151	0.151	0.151	0.151	0.151	0.136	0.136
0.102	0.096	0.181	0.210	0.210	0.210	0.210	0.132	0.132
0.094	0.075	0.126	0.246	0.246	0.246	0.246	0.160	0.160
0.068	0.055	0.130	0.198	0.198	0.198	0.198	0.087	0.087
0.062	0.027	0.159	0.25	0.25	0.25	0.25	0.130	0.130
0.090	0.034	0.181	0.174	0.174	0.174	0.174	0.082	0.082
							2.790091597	
							1.693554271	
							1.610516916	
							1.243761396	
							0.893836782	
							0.871870743	
							0.836994098	
							0.720265728	
							0.682464643	
							0.656643826	

Table 21 Popularity of topics in Sweden

Topic		2020			2021			P <sub>K</sub>
	Vaccine	P <sub>January &amp; February</sub>			P <sub>May &amp; June</sub>			P <sub>K</sub>
	Death	P <sub>March &amp; April</sub>			P <sub>July &amp; August</sub>			P <sub>K</sub>
	Economy	P <sub>September &amp; October</sub>			P <sub>September &amp; October</sub>			P <sub>K</sub>
	Students	P <sub>November &amp; December</sub>			P <sub>January &amp; February</sub>			P <sub>K</sub>
0.085	0.234	0.153	0.140	0.140	0.188	0.188	0.188	0.2044706856
0.084	0.245	0.165	0.108	0.108	0.188	0.188	0.188	1.839949948
0.102	0.225	0.161	0.117	0.117	0.188	0.188	0.188	1.666957166
0.089	0.184	0.136	0.125	0.125	0.188	0.188	0.188	1.639682297
0.074	0.172	0.149	0.132	0.132	0.188	0.188	0.188	
0.052	0.120	0.141	0.188	0.188	0.188	0.188	0.188	
0.057	0.136	0.151	0.151	0.151	0.188	0.188	0.188	
0.102	0.096	0.181	0.210	0.210	0.188	0.188	0.188	
0.094	0.075	0.126	0.246	0.246	0.188	0.188	0.188	
0.068	0.055	0.130	0.198	0.198	0.188	0.188	0.188	
0.062	0.027	0.159	0.25	0.25	0.188	0.188	0.188	
0.090	0.034	0.181	0.174	0.174	0.188	0.188	0.188	

	Masking						1.609481583
	Plasma						0.96584073
	Voluntary						0.641994092
	Politics						0.561283011
Telecommuting							0.556268936
Spread							0.473835381
0.042	0.055	0.106	0.063	0.063	0.055		
0.042	0.047	0.117	0.061	0.061	0.066		
0.098	0.044	0.098	0.053	0.049	0.049		
0.154	0.059	0.071	0.071	0.041	0.065		
0.143	0.063	0.114	0.051	0.063	0.034		
0.183	0.041	0.136	0.036	0.062	0.036		
0.151	0.020	0.167	0.057	0.057	0.047		
0.210	0.017	0.062	0.017	0.045	0.056		
0.246	0.031	0.082	0.025	0.025	0.044		
0.198	0.037	0.180	0.024	0.037	0.068		
0.076	0.034	0.256	0.041	0.027	0.062		
0.090	0.020	0.272	0.055	0.020	0.055		

**Table 22 Popularity of topics in Brazil**

Plasma							
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Table 23 Popularity of topics in Iran

Topic	Death	2020				2021				$P_K$
		p January & February	p March & April	p May & June	p July & August	p September & October	p November & December			
Plasma	0.0537									
Telecommuting	0.07857	0.1	0.08	0.07333	0.08	0.06666	0.11333	0.13333	0.19333	0.0537
Economy	0.07462	0.07142	0.09285	0.09285	0.09285	0.07857	0.11428	0.13571	0.14285	0.0674
Students	0.06349	0.08955	0.08208	0.08955	0.07462	0.07462	0.13432	0.09701	0.20149	0.0704
Masking	0.08148	0.08730	0.09523	0.06349	0.07142	0.08730	0.07142	0.15079	0.15873	0.0780
Voluntary	0.05128	0.04274	0.05983	0.07692	0.06838	0.11966	0.07692	0.11111	0.17949	0.0344
Plasma	0.04	0.06	0.08	0.06	0.12	0.09	0.1	0.11	0.14	0.0463
	0.08910	0.02970	0.03960	0.06930	0.12871	0.04950	0.10891	0.11881	0.24752	0.0483
	0.07865	0.06742	0.06742	0.06742	0.05618	0.07865	0.07865	0.11236	0.17978	0.0510
	0.07228	0.03614	0.04819	0.09638	0.07228	0.10843	0.10843	0.14457	0.02409	0.0372
	0.02899	0.05797	0.04348	0.07246	0.07246	0.10145	0.11594	0.18841	0.04348	0.0887
										0.797436519
										0.806300745
										0.87886753
										1.000943413
										1.045641256
										1.533499335
										1.536604201
										2.494874489

Table 24 Popularity of topics in Russia

	2020	2021	
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	Topic							
	Vaccine	Plasma	Telecommuting	Voluntary	Death	Politics	Spread	Masking
0.125	0.132	p January & February						
0.117	0.134	p March & April						
0.109	0.151	p May & June						
0.123	0.146	p July & August						
0.113	0.146	p September & October						
0.090	0.181	p November & December						
0.123	0.181	p January & February						
0.095	0.123	p March & April						
0.071	0.122	p May & June						
0.117	0.148	p July & August						
0.140	0.183	p September & October						
0.114	0.157	p November & December						
								P_K
								3.247615433
								2.036061656
								1.083736918
								1.045090318
								0.985921275
								0.776561064
								0.75863219
								0.738544267
								0.733049264
								0.594787615

Table 25 Popularity of topics in South Korea

Topic	2020		2021		P_K
	Vaccine	Masking	Vaccine	Masking	
0.1139	0.0632	0.0759	0.0759	0.0379	0.0506
0.1486	0.0540	0.0270	0.0270	0.0540	0.0405
0.114	0.157				1.810094581
					1.350502848

Table 26 Popularity of topics in Spain

Voluntary					
Students					
Spread					
0.02919	0.10948	0.08759	0.10218		
0.04929	0.09859	0.09859	0.08450		
0.072	0.096	0.064	0.064		
0.05405	0.09909	0.05405	0.09909		
0.08491	0.15094	0.04717	0.0566		
0.09917	0.08264	0.09917	0.06612		
0.09804	0.04902	0.07843	0.05882		
0.11764	0.07843	0.05882	0.04902		
0.05319	0.03191	0.07446	0.07446		
0.01176	0.08235	0.09412	0.09412		
0.04109	0.08219	0.04109	0.04109		
0.01471	0.05882	0.05882	0.05882		
				0.88348977	
				0.856340263	
				0.848863688	
				0.725070366	

Table 27 Popularity of topics in Switzerland

Table 28 Popularity of topics in Turkey

Topic	2020				2021				$P_K$
	Vaccine	Death	Telecommuting	Economy	Spread	Politics	Masking	Students	
Plasma	0.032	0.064	0.056	0.088	0.088	0.129	0.120	0.112	0.185
Vaccine	0.058	0.049	0.049	0.137	0.088	0.098	0.137	0.107	0.098
Death	0.060	0.034	0.078	0.086	0.086	0.130	0.104	0.086	0.113
Telecommuting	0.104	0.034	0.069	0.034	0.093	0.162	0.127	0.093	0.116
Economy	0.071	0.023	0.083	0.059	0.083	0.142	0.190	0.083	0.107
Spread	0.091	0.068	0.045	0.068	0.114	0.126	0.114	0.068	0.137
Politics	0.061	0.098	0.037	0.086	0.074	0.111	0.111	0.061	0.098
Masking	0.083	0.083	0.027	0.083	0.097	0.097	0.111	0.097	0.069
Students	0.055	0.097	0.083	0.041	0.055	0.111	0.041	0.125	0.097
Voluntary	0.014	0.074	0.119	0.074	0.029	0.089	0.104	0.104	0.089
Plasma	0.032	0.096	0.080	0.096	0.048	0.048	0.096	0.096	0.112
Vaccine	0.063	0.063	0.127	0.063	0.042	0.042	0.085	0.063	0.085
Death	0.731615425				0.790528942		0.858665746		1.329151954
Telecommuting	0.14285	0.08571	0.25714	0.25714	0.25714	0.25714	0.25714	0.25714	1.271427027
Economy	0.12121	0.12121	0.33333	0.33333	0.33333	0.33333	0.33333	0.33333	3.405293167
Spread	0.07921	0.11881	0.29703	0.29703	0.29703	0.29703	0.29703	0.29703	0.922944748
Politics	0.06315	0.09473	0.30526	0.30526	0.30526	0.30526	0.30526	0.30526	1.246397344
Masking	0.08333	0.12037	0.24074	0.24074	0.24074	0.24074	0.24074	0.24074	1.28952785
Students	0.07547	0.14150	0.21698	0.21698	0.21698	0.21698	0.21698	0.21698	2.809276003

Table 29 Popularity of topics in Netherlands

Topic	2020				2021				$P_K$
	Vaccine	Telecommuting	Politics	Other	Vaccine	Telecommuting	Politics	Other	
Vaccine	0.11111	0.14141	0.25252	p January & February	0.058	0.049	0.049	0.049	0.176
Telecommuting	0.08333	0.12037	0.24074	p March & April	0.060	0.034	0.078	0.086	0.217
Politics	0.06315	0.09473	0.30526	p May & June	0.104	0.034	0.069	0.093	0.162
Other	0.07921	0.11881	0.29703	p July & August	0.071	0.023	0.083	0.059	0.154
Vaccine	0.07955	0.09091	0.36364	p September & October	0.091	0.068	0.045	0.068	0.259
Telecommuting	0.10112	0.10112	0.32584	p November & December	0.061	0.098	0.037	0.086	0.25
Politics	0.09836	0.08196	0.32786	p January & February	0.083	0.083	0.027	0.083	0.25
Other	0.14583	0.125	0.20833	p March & April	0.055	0.097	0.083	0.041	0.291
Vaccine	0.17021	0.10638	0.2766	p May & June	0.014	0.074	0.119	0.074	0.298
Telecommuting	0.14285	0.08571	0.25714	p July & August	0.032	0.096	0.080	0.096	0.290
Politics	0.12121	0.12121	0.33333	p September & October	0.063	0.063	0.127	0.063	0.361
Other				p November & December					

	Masking						
	Death						
	Spread						
	Economy						
	Plasma						
	Students						
	Voluntary						
0.0869	0.0652	0.1086	0.1521	0.1195	0.1304	0.1086	P January & February
0.0705	0.0823	0.0941	0.1176	0.1529	0.1058	0.1411	P March & April
0.0833	0.0833	0.0937	0.1145	0.125	0.1145	0.1770	P May & June
0.0833	0.0595	0.0833	0.1547	0.0952	0.0952	0.2261	P July & August
0.0694	0.0972	0.0833	0.0833	0.125	0.125	0.2916	P September & October
0.0571	0.0857	0.0571	0.0857	0.0571	0.0857	0.3714	P November & December
0.0289	0.1014	0.0434	0.0434	0.1014	0.1014	0.4347	P January & February
0.1081	0.0810	0.0540	0.0540	0.1351	0.1351	0.2432	P March & April
0.0645	0.0322	0.0645	0.0322	0.1290	0.1935	0.2580	P May & June
0.0769	0.0769	0.1153	0.1153	0.0769	0.1153	0.2307	P July & August
0.1304	0.0434	0.0869	0.0434	0.1304	0.0434	0.3478	P September & October
0.1666	0.0833	0.0416	0.1666	0.0833	0.125	0.1666	P November & December
							$P_K$
							2.997593523
							1.370848524
							1.163533751
							1.026432996
							0.926429071
							0.891887075
							0.718527288
							0.741650658
							0.908693219
							0.899833742
							0.752407523
							0.923953233
							1.049062189

Table 30 Popularity of topics in Belgium

Topic	2020				2021				$P_K$
	Vaccine	Telecommuting	Death	Masking	Economy	Spread	Politics		
0.0869	0.0652	0.1086	0.1521	0.1195	0.1304	0.1086	P January & February		
0.0705	0.0823	0.0941	0.1176	0.1529	0.1058	0.1411	P March & April		
0.0833	0.0833	0.0937	0.1145	0.125	0.1145	0.1770	P May & June		
0.0833	0.0595	0.0833	0.1547	0.0952	0.0952	0.2261	P July & August		
0.0694	0.0972	0.0833	0.0833	0.125	0.125	0.2916	P September & October		
0.0571	0.0857	0.0571	0.0857	0.0571	0.0857	0.3714	P November & December		
0.0289	0.1014	0.0434	0.0434	0.1014	0.1014	0.4347	P January & February		
0.1081	0.0810	0.0540	0.0540	0.1351	0.1351	0.2432	P March & April		
0.0645	0.0322	0.0645	0.0322	0.1290	0.1935	0.2580	P May & June		
0.0769	0.0769	0.1153	0.1153	0.0769	0.1153	0.2307	P July & August		
0.1304	0.0434	0.0869	0.0434	0.1304	0.0434	0.3478	P September & October		
0.1666	0.0833	0.0416	0.1666	0.0833	0.125	0.1666	P November & December		
							$P_K$		
							2.997593523		
							1.370848524		
							1.163533751		
							1.026432996		
							0.926429071		
							0.891887075		

Table 31 Popularity of topics in Denmark

		2020					2021																																																																																																																										
		Topic		Vaccine					Politics			Masking																																																																																																																					
		Death		Spread			Telecommuting		Students			Economy																																																																																																																					
		P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	P <sub>7</sub>	P <sub>8</sub>	P <sub>9</sub>	P <sub>10</sub>	P <sub>11</sub>	P <sub>12</sub>																																																																																																																				
Voluntary	Plasma	0.05208	0.07291	0.09375	0.09333	0.11458	0.13541	0.22916	P January & February	0.02739	0.04109	0.05479	0.06849	0.08333	0.11627	0.22093	P March & April	0.03488	0.05814	0.06976	0.09302	0.08139	0.11627	0.15116	0.21917	P May & June	0.01428	0.05714	0.04285	0.1	0.05714	0.04285	0.14285	0.18571	0.27142	P July & August	0.02857	0.08571	0.05714	0.04286	0.07143	0.1	0.08571	0.08571	0.35714	P September & October	0.10959	0.0411	0.06849	0.0411	0.05479	0.06849	0.05479	0.05479	0.06849	P November &	0.06452	0.06452	0.08065	0.01613	0.04839	0.09677	0.08065	0.04839	0.04839	0.45161	P January & February	0.11166	0.06666	0.06666	0.03333	0.06666	0.06666	0.1	0.01666	0.03333	0.43333	P March & April	0.02941	0.08823	0.08823	0.08823	0.08823	0.08823	0.17647	0.11764	0.05882	0.17647	P May & June	0.06897	0.06897	0.13793	0.13793	0.06897	0.10345	0.06897	0.10345	0.10345	P July & August	0.03846	0.03846	0.03846	0.07692	0.07692	0.11538	0.15384	0.03846	0.15384	P September & October	0.05	0.1	0.05	0.05	0.05	0.15	0.15	0.15	0.05	P November &	0.634832115	0.762116937	0.747318051	0.840539206	0.926729366	1.31412043	1.181020773	1.190140779	3.539263962	P <sub>K</sub>

Table 32 Popularity of topics in Chile

Table 33 Popularity of topics in Saudi Arabia

	Vaccine						
	Telecommuting						
	Spread						
	Politics						
	Death						
	Economy						
	Plasma						
	Masking						
	Voluntary						
	Students						
0.084	0.118	0.152	0.186	p January & March & April	0.0375	0.05	0.1
0.109	0.145	0.145	0.218	p March & April	0.06153	0.03076	0.07692
0.063	0.127	0.127	0.276	p May & June	0.09803	0.05882	0.07843
0.102	0.163	0.142	0.204	p July & August	0.08163	0.14285	0.08163
0.086	0.173	0.086	0.173	p September & October	0.06122	0.08163	0.08163
0.075	0.1	0.125	0.275	p November & December	0.0476	0.0714	0.0476
0.028	0.085	0.057	0.428	p January & February	0.0238	0.0472	0.0462
0.047	0.095	0.095	0.285	p March & April	0.10526	0.07894	0.02631
0.125	0.062	0.031	0.343	p May & June	0.03030	0.06060	0.03030
0.041	0.125	0.083	0.333	p July & August	0.08	0.04	0.08
0.153	0.076	0.192	0.230	p September & October	0.04166	0.04166	0.08333
0.15	0.05	0.2	0.2	p November & December	0.16667	0.04167	0.04167
							3.156351195
							1.439742135
							1.324311995
							1.068367094
							0.746016938
							0.835262913
							0.910912663
							0.967250725
							1.083087724
							1.29311518
							1.33164867
							3.304598799

Table 34 Popularity of topics in Peru

	Topic	2020	2021	$P_K$
	Vaccine			
	Death			
	Telecommuting			
	Masking			
0.084	0.118	0.152	0.186	0.314202161
0.109	0.145	0.145	0.218	0.746016938
0.063	0.127	0.127	0.276	0.813904228
0.102	0.163	0.142	0.204	0.910912663
0.086	0.173	0.086	0.173	0.967250725
0.075	0.1	0.125	0.275	1.083087724
0.028	0.085	0.057	0.428	1.29311518
0.047	0.095	0.095	0.285	1.33164867
0.125	0.062	0.031	0.343	3.304598799
0.041	0.125	0.083	0.333	
0.153	0.076	0.192	0.230	
0.15	0.05	0.2	0.2	

Politics						
Students						
Spread						
Voluntary						
Economy						
Plasma						

Table 35 Popularity of topics in Portugal

		2020				2021					
		Topic									
Topic	Category	Value		Date		Value		Date		P_K	
		P	M	S	A	P	M	S	O		
Economy	Vaccine	0.0769	0.0256	0.0512	0.1025	0.1282	0.0769	0.1282	0.1794	P January & February	
	Telecommuting	0.0454	0.0454	0.0909	0.1136	0.0909	0.0681	0.1136	0.1363	P March & April	
	Death	0.0232	0.0697	0.0697	0.0930	0.1162	0.1395	0.0697	0.1860	P May & June	
	Politics	0.0487	0.0731	0.0975	0.1219	0.0731	0.1219	0.1219	0.0487	P July & August	
	Masking	0.0555	0.1111	0.0555	0.0277	0.0555	0.0833	0.0833	0.1111	P September & October	
	Spread	0.1290	0.1612	0.0322	0.0322	0.0322	0.1290	0.0322	0.0322	P November & December	
	Voluntary	0.0977	0.0322	0.0642	0.0645	0.0967	0.0967	0.0645	0.1290	P January & February	
Plasma	Vaccine	0.0285	0.0857	0.0571	0.0285	0.0285	0.0857	0.1428	0.3428	P March & April	
	Telecommuting	0.0571	0.0571	0.0857	0.0857	0.0571	0.1142	0.0571	0.3142	P May & June	
	Death	0.0740	0.0370	0.0370	0.1111	0.0370	0.1111	0.0740	0.1481	P July & August	
	Politics	0.0434	0.1304	0.0434	0.0434	0.0434	0.0869	0.0869	0.1739	P September & October	
	Masking	0.05	0.05	0.1	0.05	0.15	0.05	0.15	0.15	P November & December	
	Spread	0.981431107	1.211654798	1.049512702	1.356901868	3.286160508	0.903173428	0.821879348	0.814756838	0.813793178	P_K

Students							
							0.760736226

Table 36 Popularity of topics in Qatar

Topic	2020				2021				$P_K$
	Vaccine	Telecommuting	Politics	Death	Spread	Masking	Plasma	Students	
0.0168 p January & February	0.0555	0.0277	0.0833	0.0555	0.1111	0.0833	0.1388	0.1111	0.1944 p January & February
0.0126 p March & April	0.0625	0.0625	0.0312	0.1562	0.125	0.125	0.1562	0.0937 p March & April	0.0681
0.0126 p May & June	0.08	0.12	0.04	0.08	0.08	0.08	0.12	0.12	0.16 p May & June
0.0210 p July & August	0.1	0.05	0.025	0.075	0.1	0.1	0.125	0.2225 p July & August	0.0243
0.0211 p September & October	0.0540	0.1351	0.0540	0.0540	0.0270	0.1081	0.0810	0.0810 p September & October	0.0833
0.0370 p November & December	0.0370	0.0740	0.0370	0.0740	0.0370	0.0740	0.0370	0.1351 p November & December	0.0645
0.0357 p January & February	0.0357	0.0357	0.1071	0.1428	0.0714	0.1071	0.0357	0.1428 p January & February	0.0322
0.1034 p January & February	0.0689	0.1379	0.1034	0.0344	0.0689	0.0344	0.0689	0.1034 p January & February	0.0857
0.0769 p March & April	0.0384	0.0769	0.1538	0.0384	0.0769	0.1153	0.0384	0.1153 p March & April	0.0857
0.0476 p May & June	0.0476	0.0476	0.0952	0.0952	0.0476	0.0952	0.1428	0.0476 p May & June	0.0740
0.1176 p July & August	0.0588	0.0588	0.0588	0.1176	0.0588	0.1764	0.1176	0.1176 p July & August	0.0434
0.0555 p September & October	0.1111	0.0555	0.0555	0.1111	0.0555	0.1111	0.1666	0.0555 p September & October	0.05
0.0042 p November & December									0.826053947
									2.84429985
									1.341119053
									1.207445498
									1.172319217
									0.985545099
									0.929702436
									0.880182017
									0.858538573
									0.826053947

Table 37 Popularity of topics in Ecuador

Topic	2020				2021				$P_K$
	Vaccine	Telecommuting	Politics	Death	Spread	Masking	Plasma	Students	
0.0295 p January & February	0.0253	0.0740	0.0370	0.0740	0.0370	0.0740	0.0370	0.1351 p January & February	0.2025
0.0084 p March & April	0.0337	0.0689	0.1379	0.1034	0.0344	0.0689	0.0344	0.1034 p March & April	
0.0126 p May & June	0.0769	0.0384	0.0769	0.1538	0.0384	0.0769	0.1153	0.0384 p May & June	
0.0042 p July & August	0.0476	0.0476	0.0952	0.0952	0.0476	0.0952	0.1428	0.0476 p July & August	
0.0042 p September & October	0.1176	0.0588	0.0588	0.1176	0.0588	0.1764	0.1176	0.1176 p September & October	
0.0042 p November & December	0.0555	0.1111	0.0555	0.1111	0.0555	0.1111	0.1666	0.0555 p November & December	

		Telecommuting		
	Death			
	Students			
	Masking			
	Spread			
	Plasma			
	Politics			
	Economy			
7171.0	Voluntary			
6575.0				
6575.0				
1080.0				
0.0843				
0.0760				
0.1308				

## Appendix 2

